

## BOWEN UNIVERSITY, IWO COLLEGE OF MANAGEMENT AND SCIENCES ECONOMICS PROGRAMME B.Sc. DEGREE 2022/2023 ACADEMIC SESSION SECOND SEMESTER EXAMINATION

Course code: ECN 104 Course credit: 3
Course title: Introductory Mathematics for Economics II Time allowed: 3 hours
Instruction: Provide your answers systematically and show your workings step by step.

## Section A: Attempt all questions in this section. Each questions attract 1 mark [25 marks]

- 1. When multiplying powers with the same base, keep the base and .....the exponents
- 2.  $x^2 + xy y = 1$  is an example of a/an ..... function
- 3. The mathematical statement that involves setting two algebraic expressions equal to each other is regarded as ......
- 4. Given Q = a + bP, identify the slope, the intercept, the dependent and independent variable of the function.
- 5. Using the exponential form, the ......of a power indicates how many times the base multiplies itself
- 6. Evaluate f(3), given  $f(x) = 4x^2 3x + 12$
- 7. The ...... of a matrix is obtained by interchanging the rows and columns of the original matrix.
- 8. The formula for the quotient rule when differentiating with respect to x is written as ...
- 9. If y = f(x) = C, where C is an arbitrary constant, then  $\frac{\partial y}{\partial x} = f'(x) = ?$
- 10. ...... is obtained by multiplying the two elements in the principal diagonal of A and then subtracting the product of the two remaining elements.
- 11. Find the value of x using the quadratic formula  $3x^2 41x + 26 = 0$

For question 12 - 16, identify the degree of each terms of the following polynomials

12. 
$$2x^3y + x^2y + 7x$$

13. 
$$10x^5y^5 + 4xy + 3$$

14. 
$$8y + x^2y + 7x$$

15. 
$$3x^2y - 41x^2 + 26$$

$$16.\ 2x^3\ y + 9x^2\ y$$

For question 17 -22, state whether the following statements are True or False

- 17. A non-linear equation is usually represented by a straight line graph
- 18. All identity matrices are square matrices
- 19. All square matrices are identity matrices
- 20. The order of a column matrix is generally denoted as r x 1.
- 21. The order of a matrix is the same as the position of each elements in a matrix

## 22. All square matrices have determinant

Solve the following exponents

23. 
$$\left(\frac{35a^5b^7}{7a^2b^3}\right)^3 =$$

$$24. \left(\frac{x^4y^6}{x^2y^2}\right) =$$

25. 
$$(7s^{-4}t^3)^{-5} =$$

## Section B: Attempt any 3 questions in this section. Each questions attract 15 marks

1. (a). Solve for the unknown in the system of equations below using either the substitution or elimination method

$$18x - y = 87$$

$$-2x + 36y = 98$$
 (5 marks)

(b). Expand the following polynomials

(i) 
$$(3x + 6y)(x^4 + 10x - 15)$$

$$(ii) \left(2x^2 + 6\right)(x - 5) \tag{5 marks}$$

(c). Solve for 
$$x$$
 in the equation  $5x + A = B$  where  $A = \begin{bmatrix} 14\\15\\6 \end{bmatrix}$  and  $B = \begin{bmatrix} 44\\15\\1 \end{bmatrix}$  (5 marks)

2. (a). With the aid of examples, explain each of the following types of matrices:

(i) Scalar matrix (ii) Diagonal matrix (iii) Upper and lower triangular matrix (iv) Symmetric matrix (v) Square matrix (10 marks)

(b) Differentiate between an implicit and an explicit function, with examples (5 marks)

3. Find the derivative of the following functions

(i) 
$$y = 2x^3 + x^2 + 7$$
 (3 marks)

(ii) 
$$y = 4x^5/(1-3x)$$
 (3 marks)

(i) 
$$y = 5x^4 (3x - 7)$$
 (3 marks)

(ii) 
$$y = (2x+3)^{10}$$
 (3 marks)

(iii) 
$$y = (4x - 2)(2x + 5y)$$
 (3 marks)

4. Given the matrices 
$$A = \begin{bmatrix} 4 & 7 & 2 \end{bmatrix}$$
,  $B = \begin{bmatrix} 6 \\ 5 \\ 1 \end{bmatrix}$  and  $C = \begin{bmatrix} 9 \\ 5 \\ 8 \end{bmatrix}$ .

a. Verify that 
$$A(B+C) = AB + AC$$
 (5 marks)

b. If 
$$K = 2$$
, prove that  $k(A + B) = kA + kB$  (5 marks)